



# Next Generation Ocean Prediction: Preparing for SWOT

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and Robert Helber<sup>1</sup>

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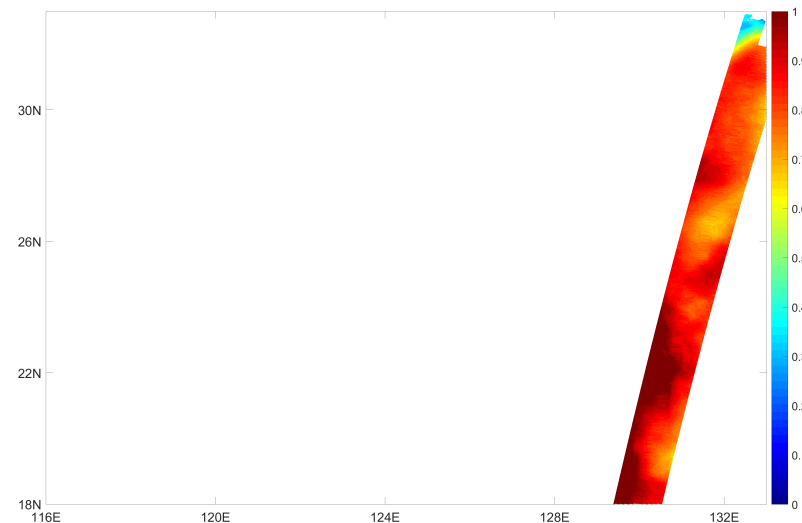
<sup>2</sup>University of New Orleans, Department of Physics, LA, USA

# Motivation & Objectives

## Motivation

- A convergence of modeling and observing capabilities is underway:
  1. 1 km regional simulations, capable of resolving submesoscale eddies, are now readily producible.
  2. The Surface Water Ocean Topography (SWOT) mission will provide the first global observations of sea surface height at horizontal resolutions capable of constraining the high resolution regional models.
- What impact will this new data provide in an operational setting?
- Using current operational technology, can submesoscale processes be constrained just by adding finer surface data?
- **What technology/assumptions need(s) to be superseded to best utilize this exciting new dataset?**

## Simulated 21-day SWOT coverage



## Question 1

How will SWOT improve ocean prediction skill when using the current operational settings?

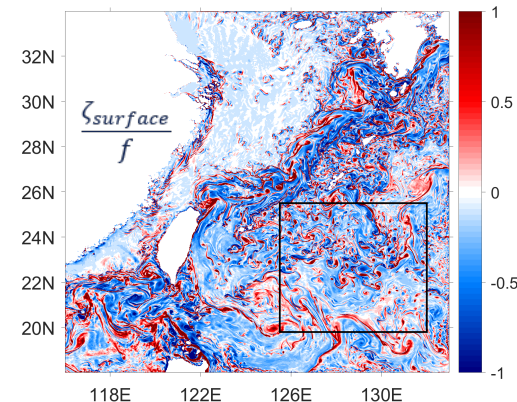
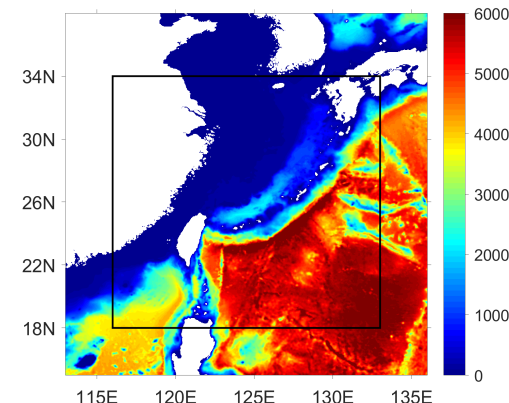
# Observing System Simulation Experiment (OSSE)

## NATURE

Dynamical Model	Navy Coastal Ocean Model (NCOM)
Horizontal Resolution	1 km
# $\sigma/z$ Layers	50
Initial Condition	December 1, 2015 3 km NCOM
Boundary Conditions	8 km HYCOM -> 3 km NCOM -> 1 km NCOM
Surface Forcing	Navy Global Environmental Model (NAVGEN)

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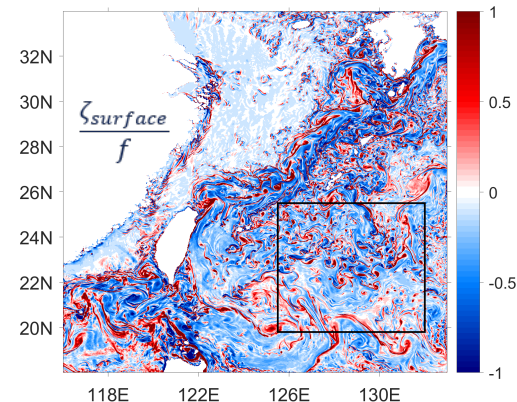
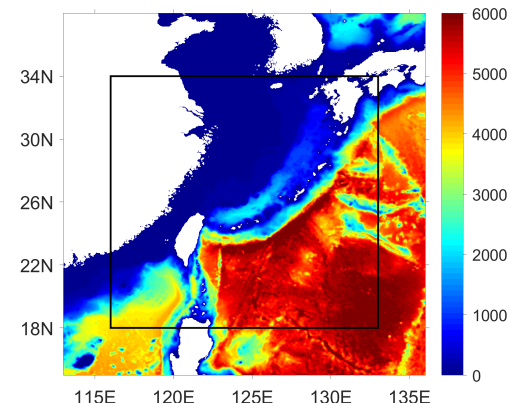
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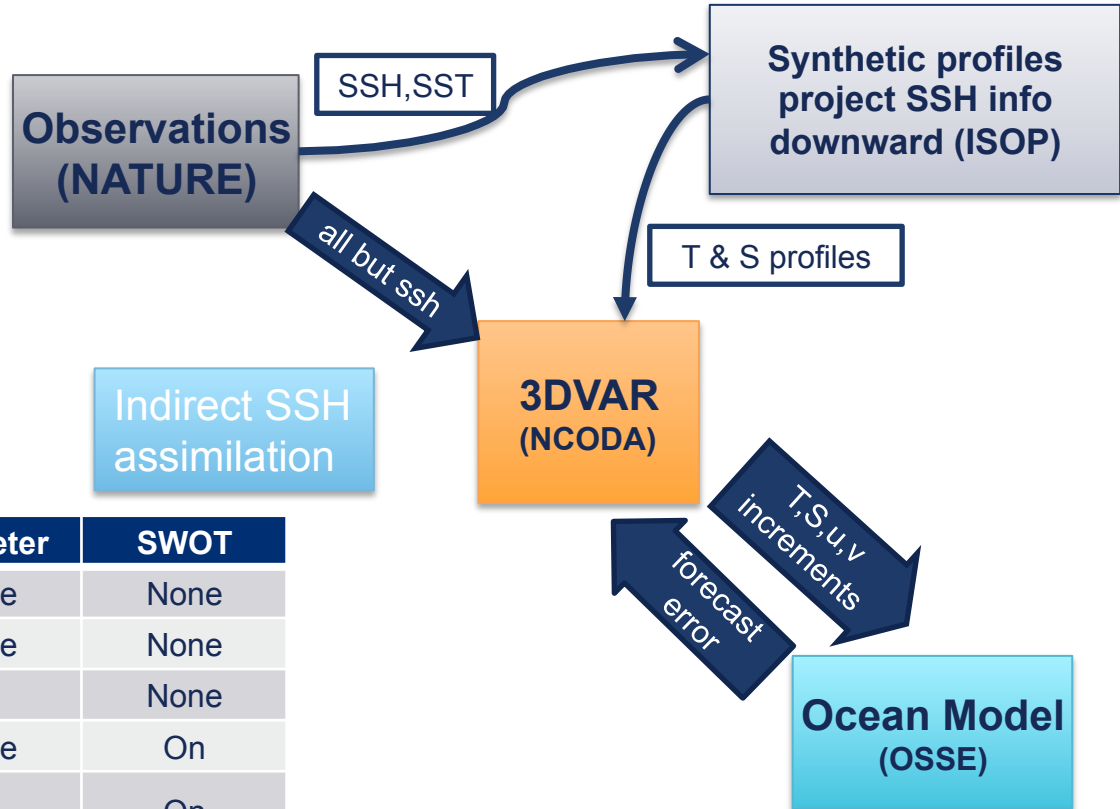
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# NCODA 3DVAR Data Assimilation

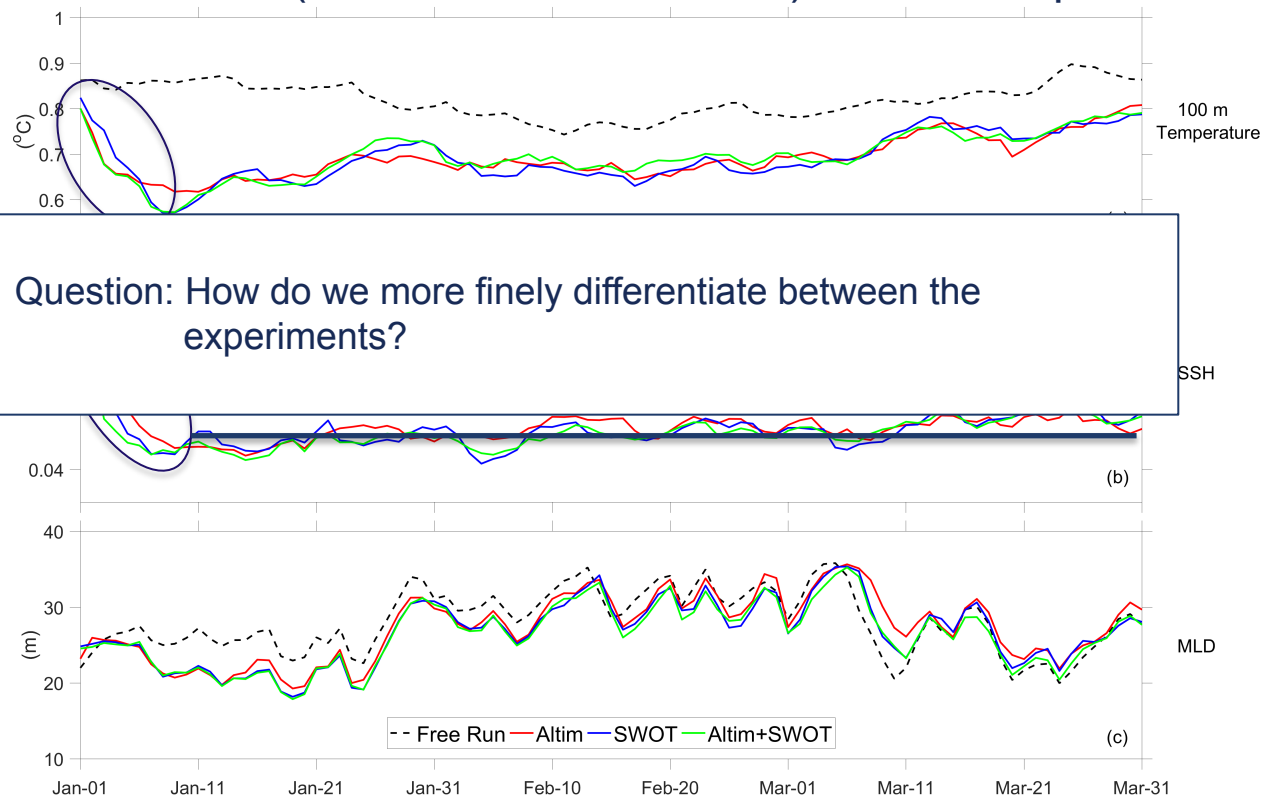
NCODA → Navy Coupled Ocean Data Assimilation  
ISOP → Improved Synthetic Ocean Profile System  
NCOM → Navy Coastal Ocean Model



	SST	<i>In Situ</i>	Altimeter	SWOT
NATURE	None	None	None	None
Free Run	None	None	None	None
Altim	On	On	On	None
SWOT	On	On	None	On
Altim + SWOT	On	On	On	On

## Area-Averaged Errors

Mean Absolute Error (NATURE minus OSSE) in water depth > 1000 m



# Wavenumber Spectra

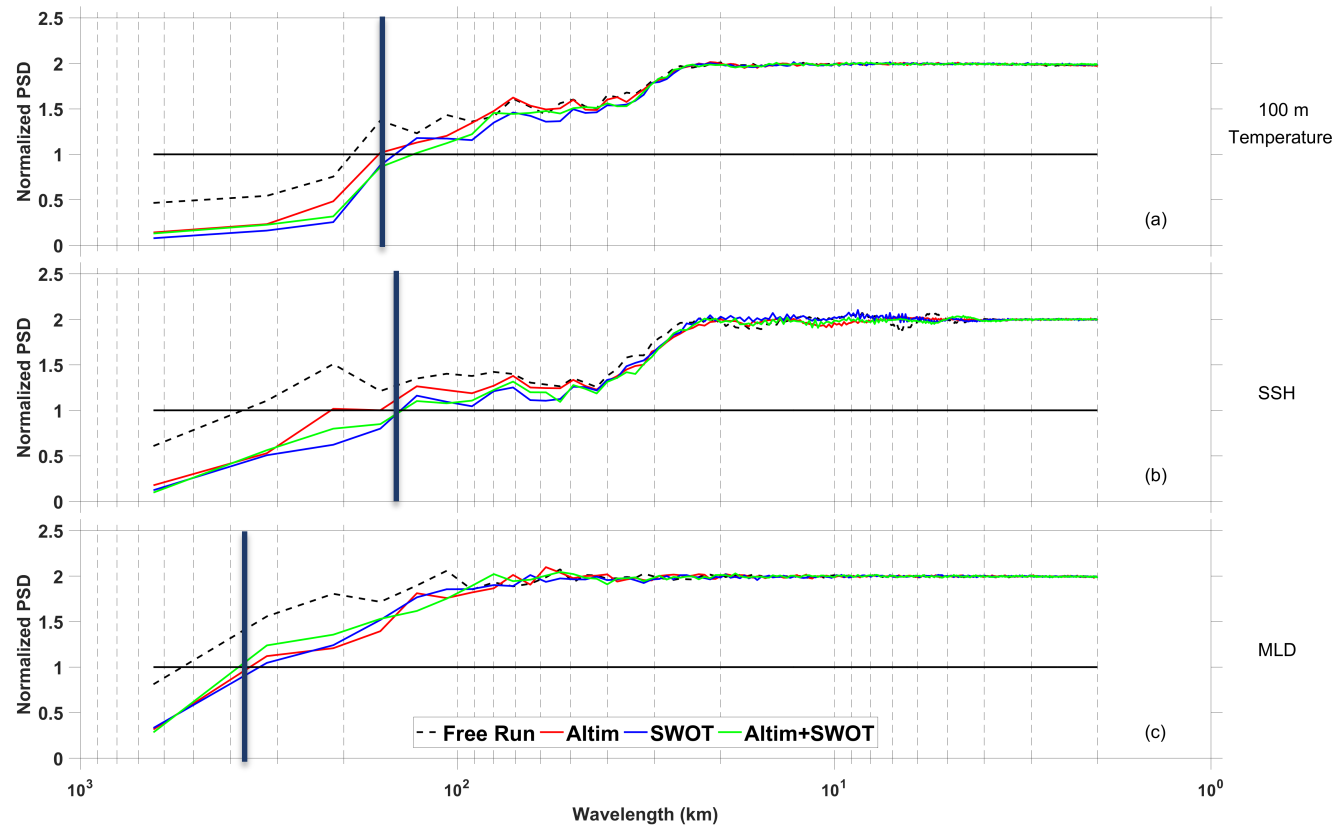
$$\frac{\epsilon_{OSSE}}{\langle \gamma_{NATURE}, \gamma_{OSSE} \rangle}$$

$\epsilon_{OSSE}$  = Spectrum of NATURE – OSSE

$\gamma_{NATURE}$  = Spectrum of NATURE

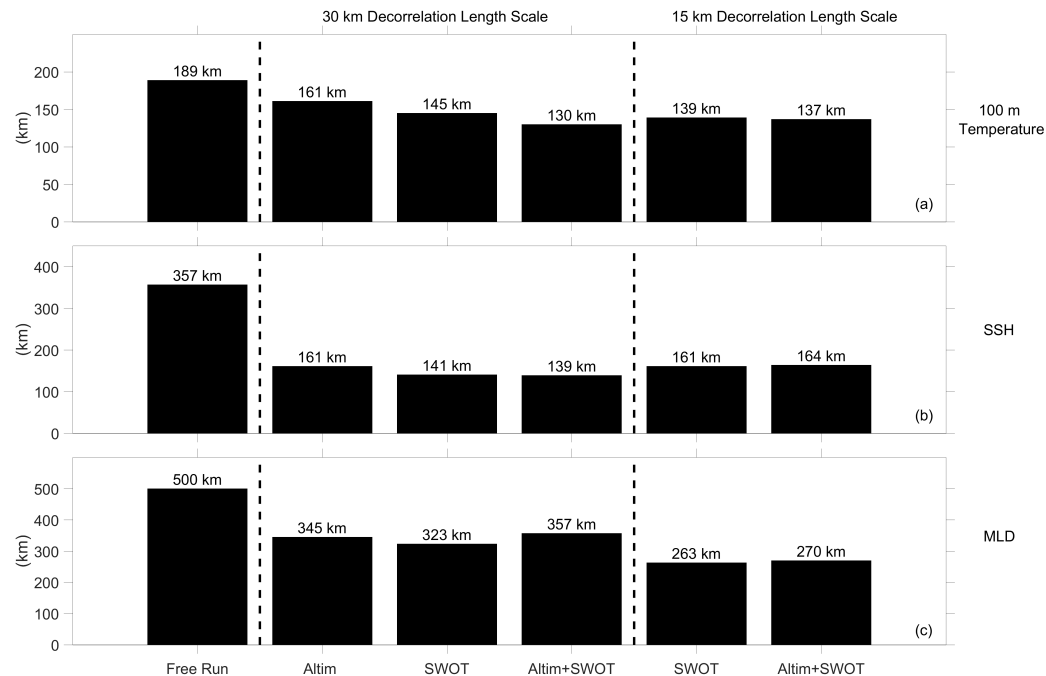
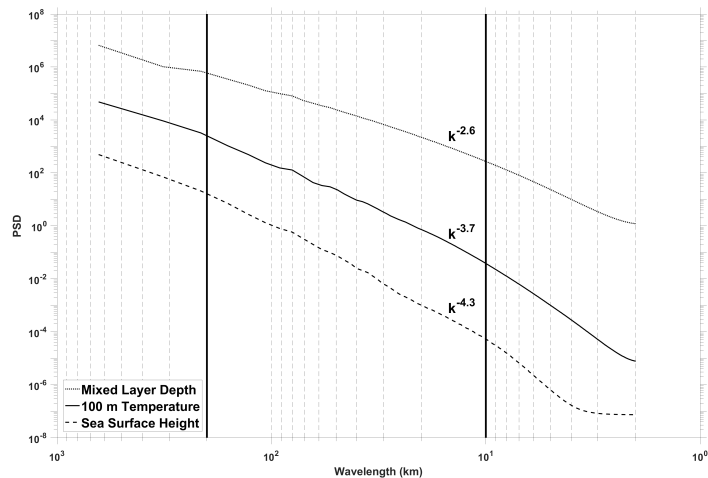
$\gamma_{OSSE}$  = Spectrum of OSSE

$\langle \rangle$  = Mean



# Wavenumber Spectra

- Variables with relatively low energy at short wavelengths feature higher errors when reducing the decorrelation length scale.
- The reverse is true for variables with relatively higher energy at short wavelengths.



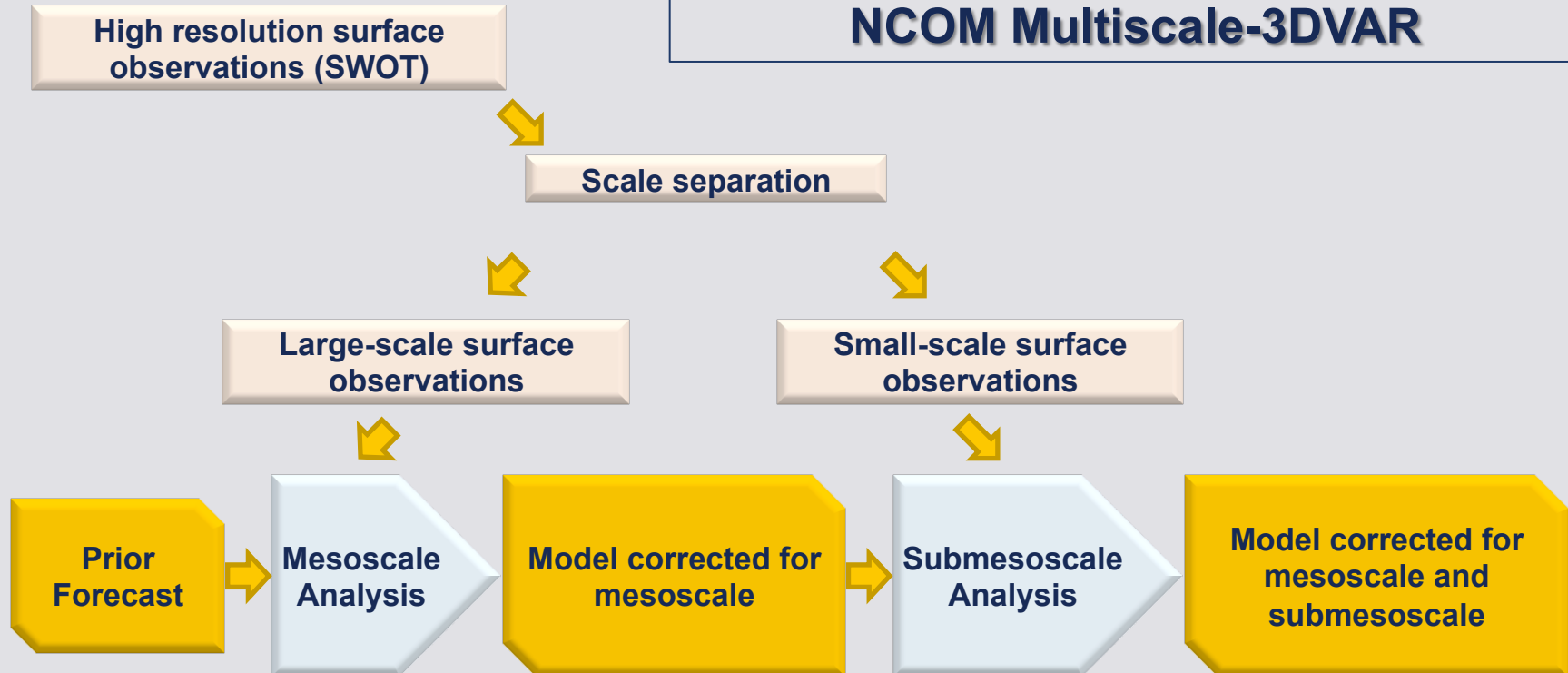
**A multiscale solution is required**

## Question 2

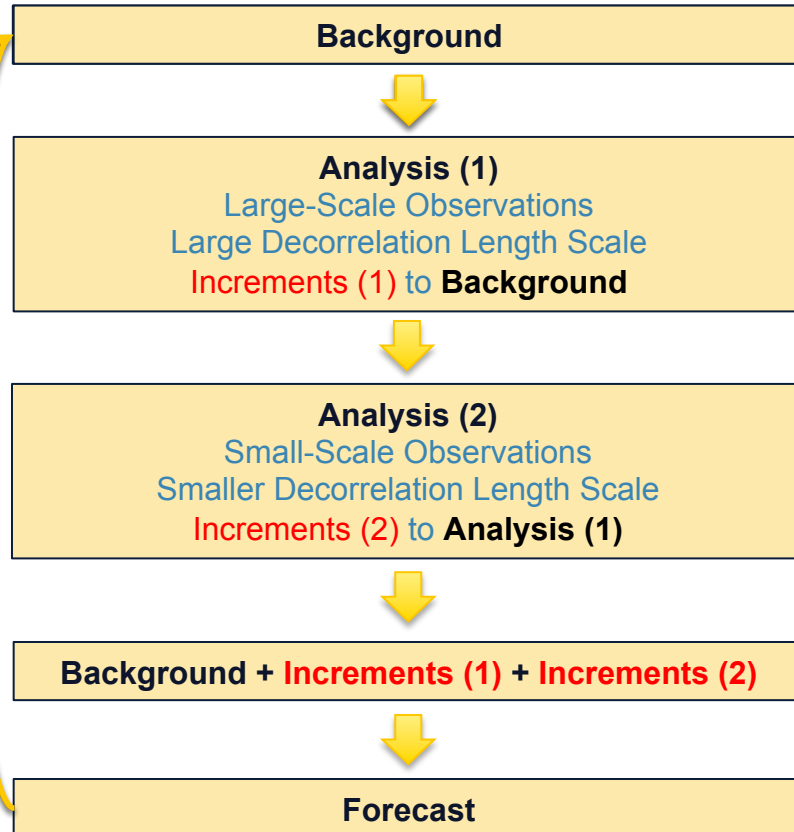
How can we extract more information from the SWOT observations without introducing scale aliasing?

# Multiscale Assimilation

## NCOM Multiscale-3DVAR



# Multiscale Assimilation



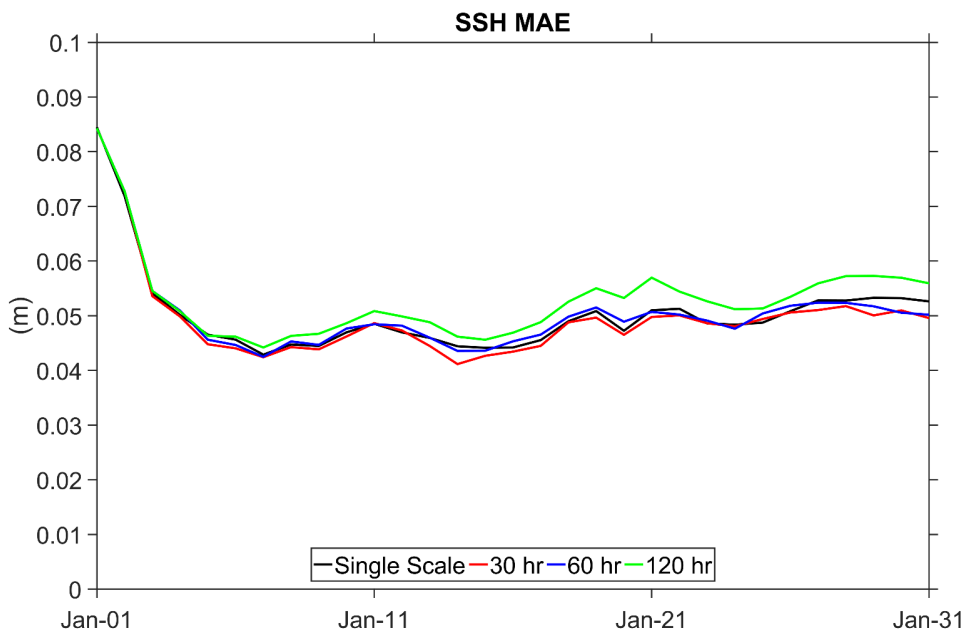
$$\begin{aligned}
 J_L(\delta \mathbf{x}_L) &= \frac{1}{2} \delta \mathbf{x}_L^T \mathbf{B}_L^{-1} \delta \mathbf{x}_L \\
 &+ \frac{1}{2} \left( \mathbf{H}^d \delta \mathbf{x}_L - \mathbf{d}_L^d \right)^T \left( \mathbf{R}_L^d \right)^{-1} \left( \mathbf{H}^d \delta \mathbf{x}_L - \mathbf{d}_L^d \right) \\
 &+ \frac{1}{2} \left( \mathbf{H}^c \delta \mathbf{x}_L - \mathbf{d}^c \right)^T \left( \mathbf{R}^s + \mathbf{H}^c \mathbf{B}_S \mathbf{H}^{cT} \right)^{-1} \left( \mathbf{H}^c \delta \mathbf{x}_L - \mathbf{d}^c \right)
 \end{aligned}$$

$$\begin{aligned}
 J_S(\delta \mathbf{x}_S) &= \frac{1}{2} \delta \mathbf{x}_S^T \mathbf{B}_S^{-1} \delta \mathbf{x}_S \\
 &+ \frac{1}{2} \left( \mathbf{H}^d \delta \mathbf{x}_S - \mathbf{d}_S^d \right)^T \left( \mathbf{R}_S^d \right)^{-1} \left( \mathbf{H}^d \delta \mathbf{x}_S - \mathbf{d}_S^d \right) \\
 &+ \frac{1}{2} \left( \mathbf{H}^c \delta \mathbf{x}_S - \mathbf{d}^c \right)^T \left( \mathbf{R}^c + \mathbf{H}^c \mathbf{B}_L \mathbf{H}^{cT} \right)^{-1} \left( \mathbf{H}^c \delta \mathbf{x}_S - \mathbf{d}^c \right)
 \end{aligned}$$

Li et al. (2015)

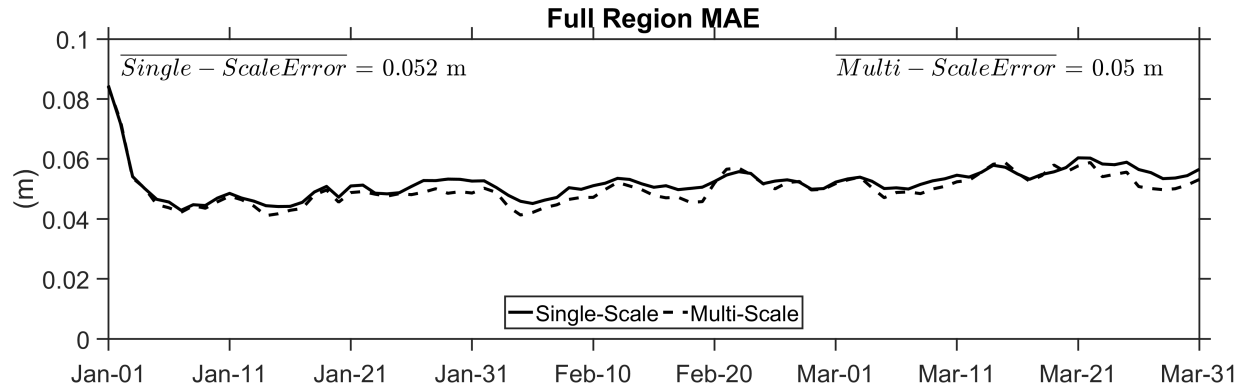


# Multiscale Assimilation

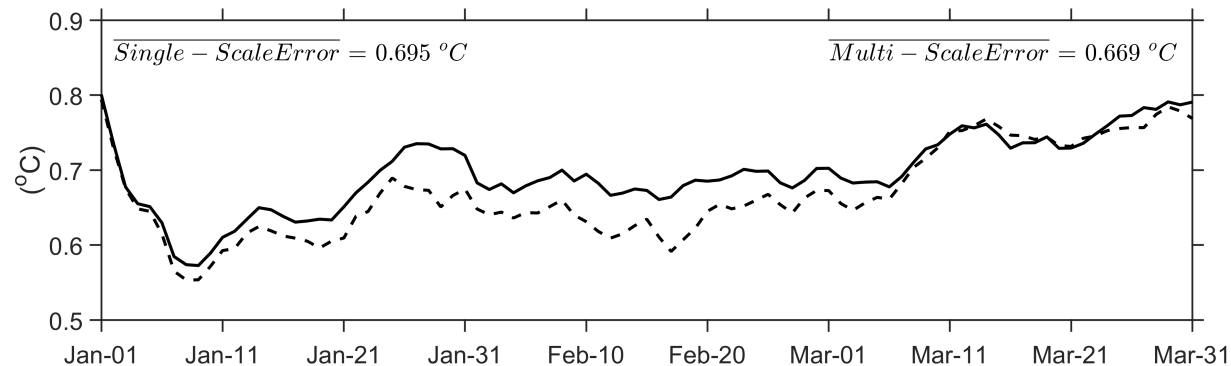


	<i>MAE</i> (cm)
Single Scale	5
Multi Scale (30 hr small-scale window)	4.94
Multi Scale (60 hr small-scale window)	5.04
Multi Scale (120 hr small-scale window)	5.3

# Multiscale Assimilation



SSH



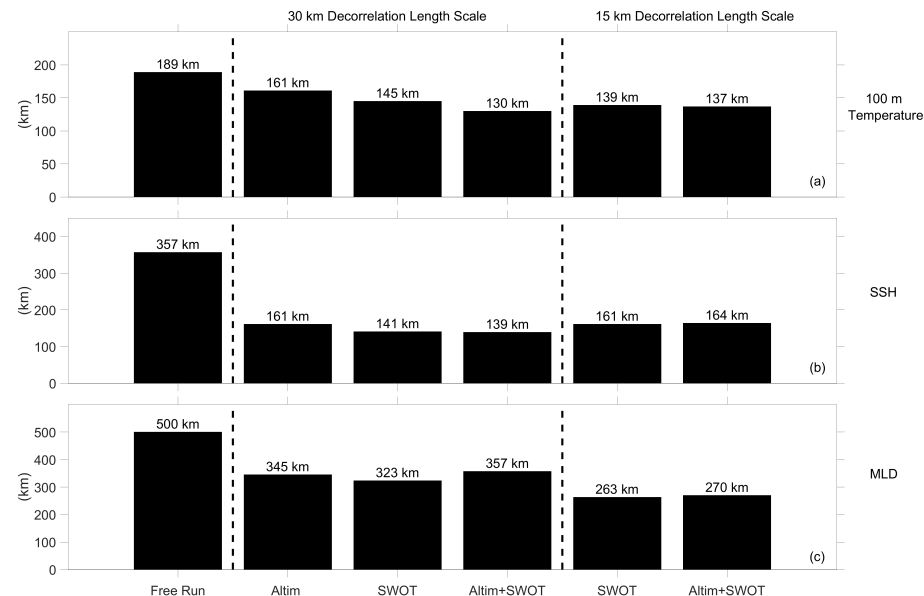
100 m  
temperature

# Summary and Conclusions

## Conclusions

- SWOT data make a considerable improvement to both analysis and forecast skill when using the current system.
- A multi-scale analysis procedure extracts additional data from the high-resolution surface observations without biasing errors into one scale or another.
- Next steps:
  1. We have taken length scales into account, but not differences in physics (i.e. we assume mesoscale dynamics in both scales).
  2. Need to implement a system that accounts for the complex SWOT error budget.

## How low can we go?

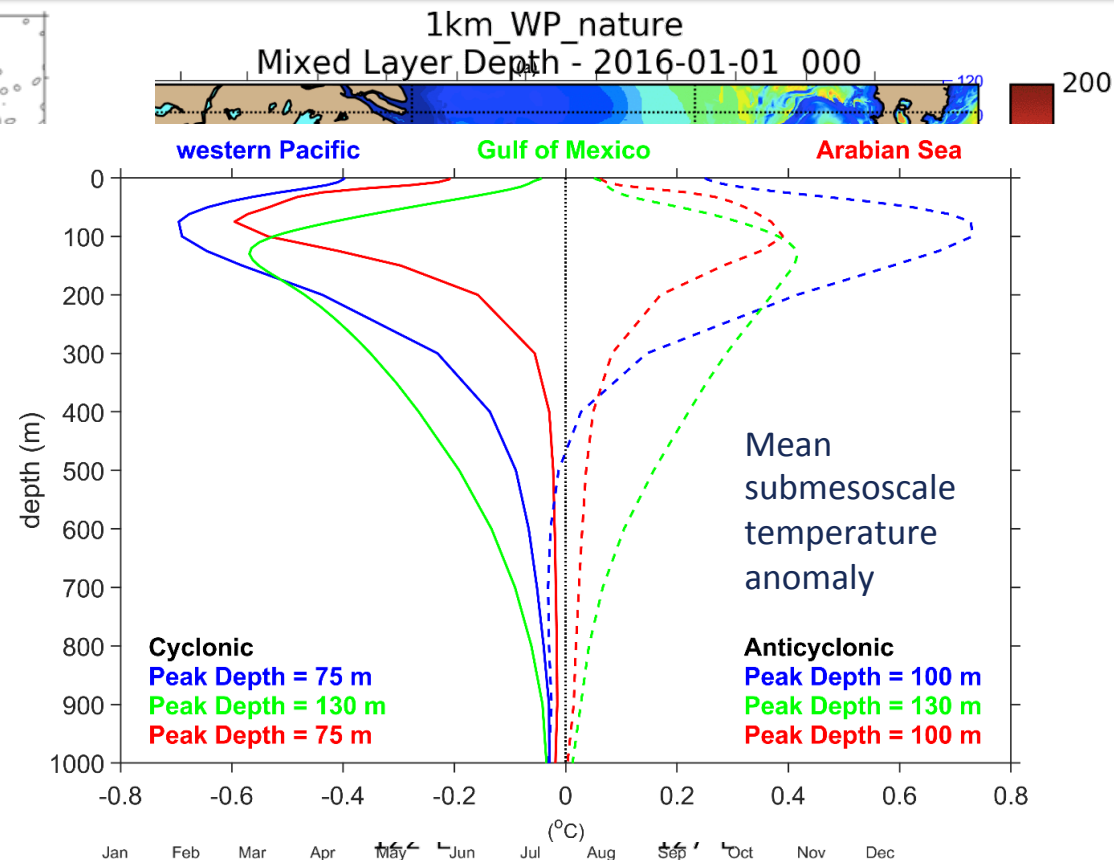
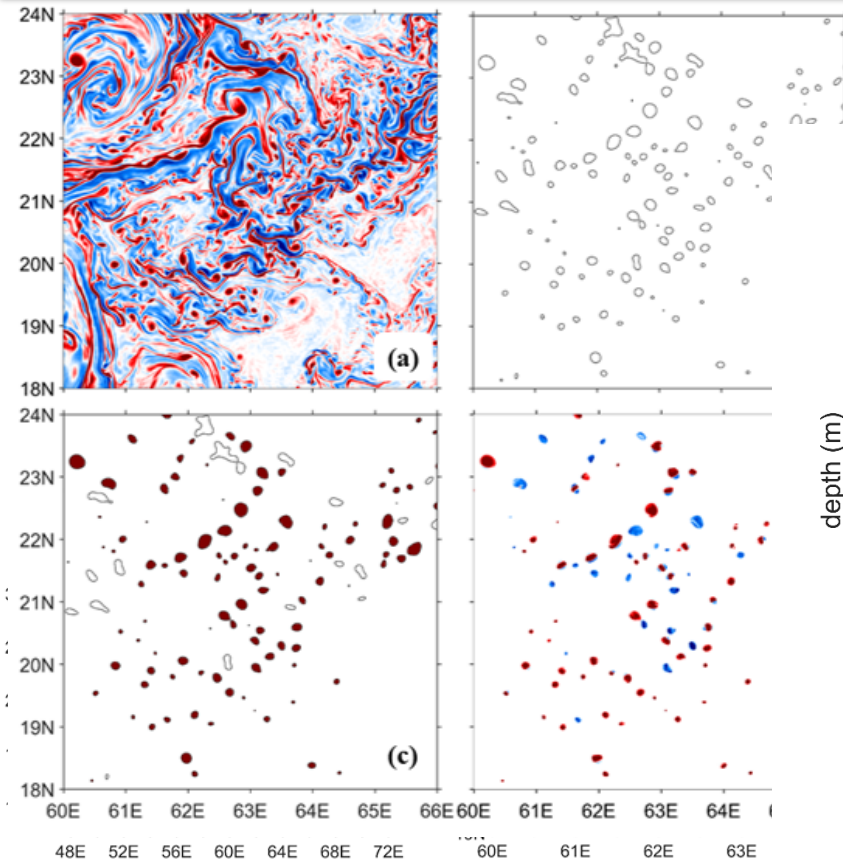


# Extra Slides

## Question 3

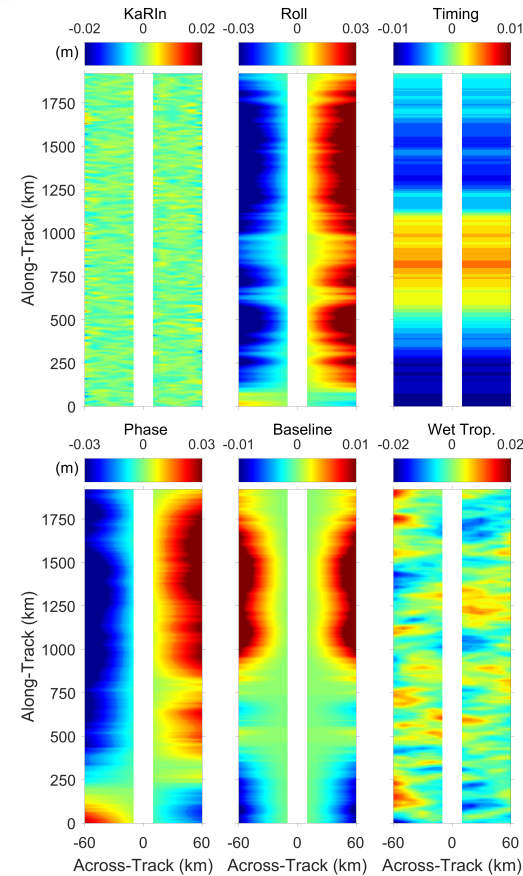
How do we account for the disparate physics found within each scale?

# Submesoscale Dynamics



## Question 4

How do we account  
for the complex  
SWOT error  
budget?



# SWOT Observation Error Covariance

$$\delta \mathbf{x}_m = \mathbf{B}_m \mathbf{H}^T (\mathbf{H} \mathbf{B}_m \mathbf{H}^T + \mathbf{R}_m)^{-1} \delta \mathbf{d}_m$$

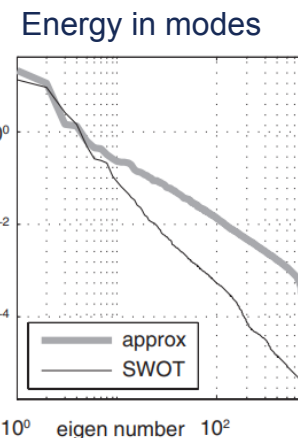
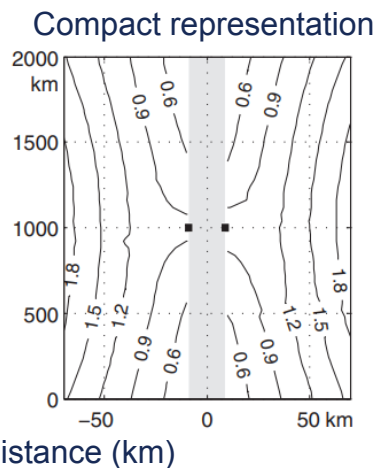
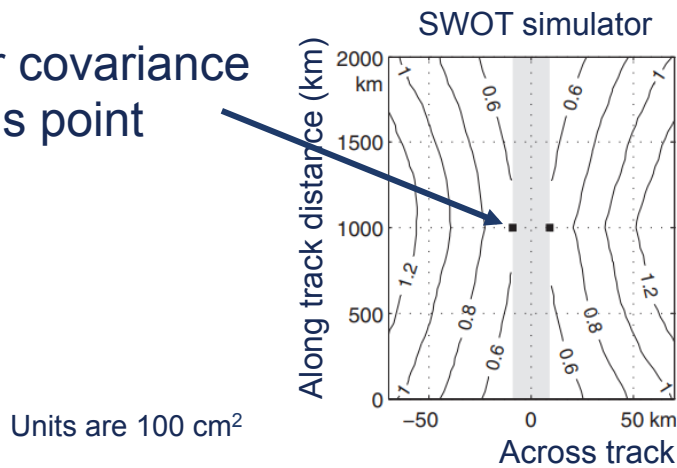
$$\delta \mathbf{x}_s = \mathbf{B}_s \mathbf{H}^T (\mathbf{H} \mathbf{B}_s \mathbf{H}^T + \mathbf{R}_s)^{-1} \delta \mathbf{d}_s$$

$\mathbf{R}$  errors contains representativeness and sensor errors

$\mathbf{R}_m$  Submesoscale, internal waves, unmodeled physics, sensor error -  $\mathbf{R}_s + \mathbf{R}_i + \mathbf{R}_u + \mathbf{R}_o$

$\mathbf{R}_s$  Submesoscale, internal waves, unmodeled physics, sensor error -  $\mathbf{R}_i + \mathbf{R}_u + \mathbf{R}_o$

Error covariance at this point



Yaremchuk, M., et al., 2018. On the approximation of the inverse error covariances of high-resolution satellite altimetry data. Quarterly Journal of the Royal Meteorological Society, 144(715), pp.1995-2000.